Multivariate Time Series:

Challenges, missing data, and forecasting

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Introduction





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Brief overview of time series data

Time series data:

- describes how something changes over time,
- is a sequential set of data points,
- □ can present temporal patterns.
- Understanding time series data enables us to make predictions, identify patterns, and make informed decisions.

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What is a multivariate time series?

Multivariate time series data:

- Evolution of several variables over time
- Different variables might influence each other
- U We might find more complex patterns, such as spatio-temporal patterns





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Challenges in analyzing time series data (1)

Complexity

- Complex systems
- Complex relationships between features
- Data quality
 - Missing data
 - Outliers
 - Noise
 - **.**...
- Non-stationary time series

High-Dimensionality







Challenges: Complexity

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- **G** Supply and demand
- Geopolitical events
- **G** Financial crises
- Pandemic
- Weather conditions
- Seasonal patterns
- **Cyclic patterns**
- **Currency** fluctuations





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Challenges: Data Quality

- The quality of data significantly impacts the reliability of data analysis, modeling, and decision-making
- Problems commonly found:
 - Missing data
 - Anomalies
 - Inconsistent sampling rates
 - Duplicate data
 - Lack of consistency in units
 - Data drift
 - Noise
 - Data quality degradation over time







Use cases

Finances

- Stock Market Analysis
- **G** Forecasting stock prices

Healthcare

- Patient monitoring
- Detecting diseases
- Urban mobility
 - □ Traffic Management
 - □ Real-time traffic forecasting
 - Optimize traffic signal timing







My research aims to **forecast traffic metrics** even in the presence of **high ratios of missing data**.





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Dealing with Missing Data





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Time series missing data

- Missing data in time series can hide existing patterns and trends
- Simple imputation methods can fail in the presence of long intervals of missing data
- Data analysis and algorithms can be affected by the existence of missing data





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How can we notice missing data?

- 'Nan' values
- Masked missing data
 - Default values out of range/ that are not possible

The number of people in Hamburg yesterday was -1

- Default values inside the range/ are possible
 - This can be dangerous depending on the context
 - This can make it difficult for us to identify missing data

The number of people in Hamburg yesterday was 0

The speed of cars between 9 a.m. and 10 a.m. yesterday was 0 km/h







What is the impact of missing data?

- We can have different percentages of missing data
- Missing data can affect one or more features
- We can have problems that are more tolerant to missing data than others
- We can have models that deal better with lower rates of missing data, while other may deal better with higher rates of missing data
- U We can have different scenarios of missing data

Missing data can affect data analysis, models, and algorithms. Having a negative impact on its applications in business and research.







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How can we handle missing data?

Before it happen

- We can prevent it from happen by monitoring our system and preventing conditions that lead to missing data
- □ However, this is not always possible!!!!

□ After it happen

- □ Ignore missing data (not a very good solution)
- Delete observations with missing data (not adequate for time series, even if we have few observations with missing data)
- Replace missing data for a value
 - O or values out of range (however, this can bring additional problems)
 - □ Mean, median, mode…
 - Simple univariate imputation techniques
 - e.g., Moving Average
 - Multivariate imputation techniques







Case study: OpenWeather dataset

- Dataset provided by OpenWeather
- Data from sensors such as temperature, pressure, humidity, wind speed, wind direction, wind gust, and cloudiness
- Data from 20 cities
- □ Hourly data from 2022







Workflow





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Generation of synthetic missing data



Overlap

t₀

p consecutive rows missing per column



p consecutive rows missing per column

Disjoint



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Generation of synthetic missing data





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Algorithms

- □ We selected the top 3 from 20 statistical methods as baseline to evaluate our algorithm:
 - **Replaced missing data using a specific value:**
 - Mean, median, last value, previous value, the nearest value, zero
 - □ Interpolation techniques:
 - Barycentric, pchip, splines, polynomial functions, piecewise polynomial, akima
- **Experimented with the KNN imputer**
- □ Propose the Focalized KNN algorithm:
 - Based on KNN imputer















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k-NN imputer

- Based on k-NN
- □ It can be used for imputation by using similar points to guess the missing data
- □ However, k-NN has some problems...
 - □ Suffers from the curse of high dimensionality
 - □ Stores the complete dataset in memory
- □ KNN imputer can be used for time series datasets; however, it does not take advantage of time series properties!!!









Spatio-temporal patterns!



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Correlation between temporal lags

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lag_0 -	1	0.87	0.63	-0.0077	-0.66	-0.041	0.84	0.97	0.85	0.98	0.85	0.97	0.84		- 0.8
lag_12 -	0.87	1	0.87	0.18	-0.61	-0.22	0.74	0.84	0.97	0.85	0.98	0.82	0.97		
lag_24 =	0.63	0.87	1	0.32	-0.49	-0.33	0.55	0.61	0.84	0.61	0.85	0.57	0.82		
lag_72 =	-0.0077	0.18	0.32	1	-0.0093	-0.66	-0.039	-0.028	0.15	-0.023	0.15	-0.044	0.13		- 0.4
lag_144 =	-0.66	-0.61	-0.49	-0.0093	1	-0.0066	-0.66	-0.63	-0.61	-0.63	-0.59	-0.63	-0.61		
lag_216 -	-0.041	-0.22	-0.33	-0.66	-0.0066	1	-0.0095	-0.028	-0.19	-0.048	-0.2	-0.029	-0.19		
iag_288 -	0.84	0.74	0.55	-0.039	-0.66	-0.0095	1	0.85	0.74	0.83	0.73	0.85	0.74		- 0.0
lag_2016 -	0.97	0.84	0.61	-0.028	-0.63	-0.028	0.85	1	0.86	0.98	0.85	0.98	0.84		
lag_2028 -	0.85	0.97	0.84	0.15	-0.61	-0.19	0.74	0.86	1	0.85	0.98	0.83	0.98		
lag_4032 =	0.98	0.85	0.61	-0.023	-0.63	-0.048	0.83	0.98	0.85	1	0.86	0.98	0.84		0.4
lag_4044 -	0.85	0.98	0.85	0.15	-0.59	-0.2	0.73	0.85	0.98	0.86	1	0.83	0.98		
lag_6048 -	0.97	0.82	0.57	-0.044	-0.63	-0.029	0.85	0.98	0.83	0.98	0.83	1	0.84		
lag_6060 -	0.84	0.97	0.82	0.13	-0.61	-0.19	0.74	0.84	0.98	0.84	0.98	0.84	1		0.8
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Focalized KNN

- Select the most correlated features
- □ Select the most relevant temporal lags
- Select the column with less missing data
 - Apply the KNN imputer for the matrix composed with:
 - the column c with missing data + correlated features + relevant temporal lags
 - □ Replace column c with the column with the imputed data
 - **Repeat until there is no more missing data**







Evaluation metrics

Mean Squared Error (MSE)

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (Y_i - \hat{Y}_i)^2$$

R²-Score

$$R^2 - Score = 1 - \frac{MSE}{MSE_{baseline}}$$



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Overlap versus Disjoint missing pattern



Discussion

Pros

- We do not need to train our algorithm
- Good with disjoint patterns
- Our solution helps with the curse of high dimensionality
- And Cons
 - Usually, it takes more time than regular KNN, especially if we have missing data affecting several columns
 - □ Not very good with overlap patterns

In the future, we would like to:

- Develop other methods to perform imputation in time series, such as methods based on Autoencoders
- Create more patterns of missing data to evaluate our models









Forecasting





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Brief overview of forecasting

- □ Forecasting is the process of making predictions about future events.
- Forecasting can be very beneficial in decision-making, planning, and risk management.
- There are different time horizons for forecasting, such as short, medium, and long-term.
- Before applying forecasting techniques, we should analyze the time series.







Forecasting methods

- Naïve methods
 - Use the last value to forecast the next one
- Statistical methods
 - AutoRegressive (AR)
 - Moving Average (MA)
 - Autoregressive Integrated Moving Average (ARIMA)
 - Seasonal ARIMA (SARIMA)
- Machine Learning methods
 - SVM
 - knn
 - LightGBM
- Deep Learning methods
 - FNN
 - GRU
 - LSTM
 - CNN







What type of learning problem is forecasting?





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Choosing the best model for forecasting methods

Most used evaluation metrics in the literature:

- Mean Absolute Error (MAE)
- Mean Absolute Percentage Error (MAPE)
- □ Root Mean Squared Error (RMSE)
- R²-Score

Cross-Validation for Time-series



Metrics based on comparing the **observed value** with the **predicted value**

Case study: Forecasting traffic flow

Dataset:

- Traffic counters deployed in Oporto, Portugal
- Data from September 30 to November 3 of 2019
- 5 minutes interval
- More than 100 sensors







Approach and Methods

- □ SARIMA
- □ FNN models
- LSTM-based models
- CNN-based models
- Hybrid LSTM-CNN models







Forecasting Pipeline





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Results and Discussion

Short-term forecasting

- SARIMA achieves a good performance
- Computationally light
- (We can also use deep learning strategies)

Long-term forecasting

- SARIMA is not suitable for long-term forecasting
- Deep learning strategies achieve good performance
- The best model was based on CNNs

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LSTMs take more time to train than CNNs or FNNs

Vehicul	ar traffic flow pred	iction using
deploye	d traffic counters i	n a city 🖈
<u>Ana Almeida</u> ^{a b}	🝳 🖾 , <u>Susana Brás ^{a b} ⊠ , Ilídio Oliveira</u>	^{a b} ⊠, <u>Susana Sargento</u> ^{a c} ⊠
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Future Work





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Future Work

- Develop a model able predict future values even in the presence of missing data
 - □ Imputation + Forecasting





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Thank you!

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